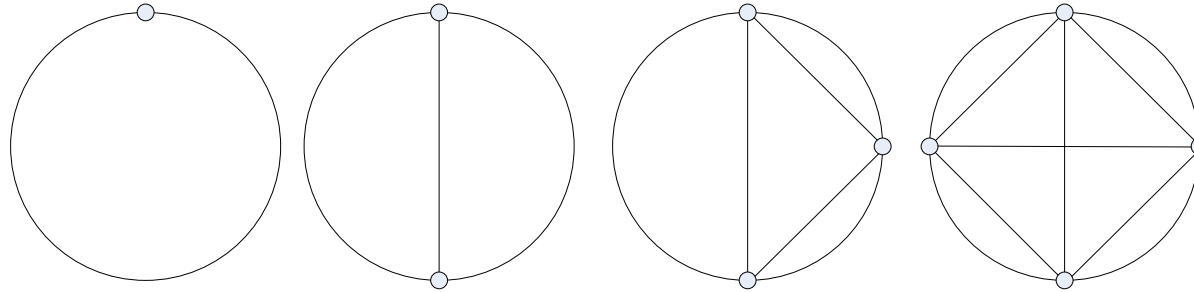


### Sequences 1



Draw a large circle. Mark the centre and draw on the diameter. Measure each  $20^\circ$  using a protractor. Put a mark (we will call them cities) on the circumference of the circle at each  $20^\circ$  angle. Join up each mark to the other marks around the circle with a straight line (we will call them roads).

How many roads are there when there is one city?

How many roads are there when there are two cities?

How many roads are there when there are 3, 4 or 5 cities?

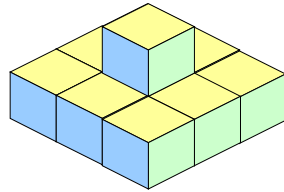
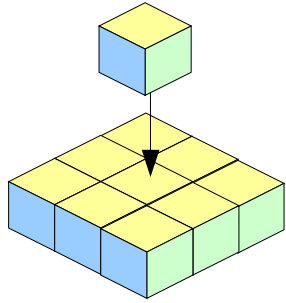
Can you use this information to work out the number of joins there will be when there are 18 cities?

What about if you had 36 cities or 72?

Can you come up with a formula to predict the number of roads for any number of cities?

***If you mark your cities as points rather than big circles, your drawing will look a lot better.***

## Sequences 2



Build a pyramid where the top most layer is 1 brick. The second layer has one brick round every edge of the top layer. The third layer has one brick around every edge of the second layer.

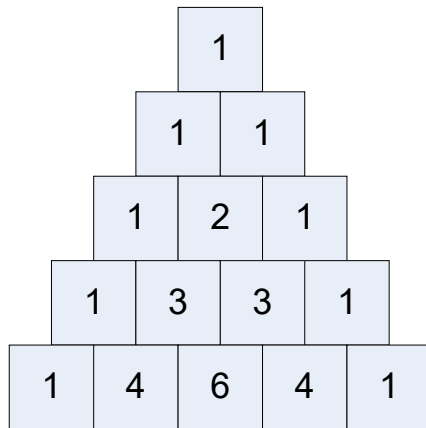
Can you work out how many bricks there are on the second layer? How many bricks are there altogether in the pyramid?

Can you work out how many bricks there are on the third layer? How many bricks are there altogether in the pyramid?

Can you work out how to find the number of bricks on any particular layer?

Can you work out how to predict the number of bricks in any sized pyramid?

## Sequences 3



Look at the triangle on the left. Each number is calculated by adding the two numbers diagonally above it.

Can you predict what the next row will read?

Can you find the total for each of the rows?

Can you find a pattern between the rows and their totals?

What will the tenth row read? What is the total on the tenth row? What is the total of all the numbers up to the tenth row?

## Sequences 4

0, 1, 1, 2, 3, 5, 8, 13, ... is called the *Fibonacci Sequence*.

Can you work out what the next term in the sequence is going to be? Can you work out the sum of all the terms up to the 1st term? What about the sum of the terms up to the second, third, fourth or fifth term?

Can you see a pattern that you can explain to your partner? Can you work out a way of predicting the 50th term? Can you work out a way of predicting the sum of all the terms up to the 50th term?

The numbers with commas between them are called **sequences**. When you add up the terms and list them in totals up to the first term, total up to the second term, total up to the third term, total up to the  $n$ th term, then that is called a **series**.

See if you can work out a formula to predict the  $n$ th term in the Fibonacci Sequence.

See if you can work out a formula to predict the  $n$ th term in the Fibonacci Series.

Using your formula, can you predict the 28th term of both the Fibonacci sequence and the series?

|     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 1   | 2   | 3   | 4   | 5   | 6   | 7   | 8   | 9   | 10  | 11  | 12  | 13  | 14  | 15  | 16  | 17  | 18  | 19  | 20  |
| 21  | 22  | 23  | 24  | 25  | 26  | 27  | 28  | 29  | 30  | 31  | 32  | 33  | 34  | 35  | 36  | 37  | 38  | 39  | 40  |
| 41  | 42  | 43  | 44  | 45  | 46  | 47  | 48  | 49  | 50  | 51  | 52  | 53  | 54  | 55  | 56  | 57  | 58  | 59  | 60  |
| 61  | 62  | 63  | 64  | 65  | 66  | 67  | 68  | 69  | 70  | 71  | 72  | 73  | 74  | 75  | 76  | 77  | 78  | 79  | 80  |
| 81  | 82  | 83  | 84  | 85  | 86  | 87  | 88  | 89  | 90  | 91  | 92  | 93  | 94  | 95  | 96  | 97  | 98  | 99  | 100 |
| 101 | 102 | 103 | 104 | 105 | 106 | 107 | 108 | 109 | 110 | 111 | 112 | 113 | 114 | 115 | 116 | 117 | 118 | 119 | 120 |
| 121 | 122 | 123 | 124 | 125 | 126 | 127 | 128 | 129 | 130 | 131 | 132 | 133 | 134 | 135 | 136 | 137 | 138 | 139 | 140 |
| 141 | 142 | 143 | 144 | 145 | 146 | 147 | 148 | 149 | 150 | 151 | 152 | 153 | 154 | 155 | 156 | 157 | 158 | 159 | 160 |
| 161 | 162 | 163 | 164 | 165 | 166 | 167 | 168 | 169 | 170 | 171 | 172 | 173 | 174 | 175 | 176 | 177 | 178 | 179 | 180 |
| 181 | 182 | 183 | 184 | 185 | 186 | 187 | 188 | 189 | 190 | 191 | 192 | 193 | 194 | 195 | 196 | 197 | 198 | 199 | 200 |
| 201 | 202 | 203 | 204 | 205 | 206 | 207 | 208 | 209 | 210 | 211 | 212 | 213 | 214 | 215 | 216 | 217 | 218 | 219 | 220 |
| 221 | 222 | 223 | 224 | 225 | 226 | 227 | 228 | 229 | 230 | 231 | 232 | 233 | 234 | 235 | 236 | 237 | 238 | 239 | 240 |
| 241 | 242 | 243 | 244 | 245 | 246 | 247 | 248 | 249 | 250 | 251 | 252 | 253 | 254 | 255 | 256 | 257 | 258 | 259 | 260 |
| 261 | 262 | 263 | 264 | 265 | 266 | 267 | 268 | 269 | 270 | 271 | 272 | 273 | 274 | 275 | 276 | 277 | 278 | 279 | 280 |
| 281 | 282 | 283 | 284 | 285 | 286 | 287 | 288 | 289 | 290 | 291 | 292 | 293 | 294 | 295 | 296 | 297 | 298 | 299 | 300 |
| 301 | 302 | 303 | 304 | 305 | 306 | 307 | 308 | 309 | 310 | 311 | 312 | 313 | 314 | 315 | 316 | 317 | 318 | 319 | 320 |

### Sequences 5

One of the most important sequences is that of prime numbers. A prime number is a number that has exactly two factors (itself and 1). The number 1 is NOT a prime number because this only has one factor.

Using the grid below, see if you can work out which numbers are prime numbers. Choose a primary colour and colour in the prime numbers in that primary colour.